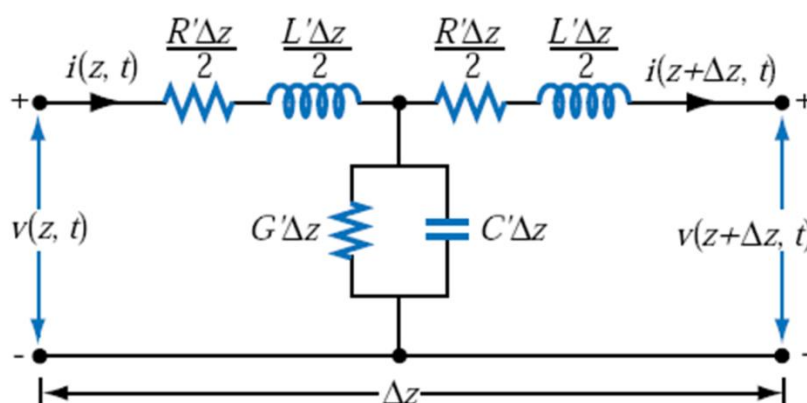




## ECE 323 - Microwave Engineering Problem Set #1

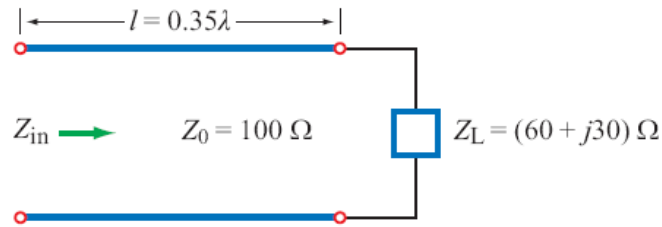
### Transmission Line Theory

- [P1] **2.1** - A  $75\ \Omega$  coaxial line has a current  $i(t, z) = 1.8 \cos(3.77 \times 10^9 - 18.13z)$  mA. Determine (a) the frequency, (b) the phase velocity, (c) the wavelength, (d) the relative permittivity of the line, (e) the phasor form of the current, and (f) the time domain voltage on the line.
- [P2] **2.2** - A T-line has the following per-unit-length parameters:  $L' = 0.5\ \mu\text{H/m}$ ,  $C' = 200\ \text{pF/m}$ ,  $R' = 4.0\ \Omega/\text{m}$ , and  $G' = 0.02\ \text{S/m}$ . Calculate the propagation constant and characteristic impedance of this line at 800 MHz. If the line is 30 cm long, what is the attenuation in dB? Recalculate these quantities in the absence of loss (i. e.,  $R' = G' = 0$ ).
- [P3] **2.7** - Show that the transmission line model (T model) shown in Fig. P3 yields the same telegrapher's equations given by Eqs. (2.2a) and (2.2b).



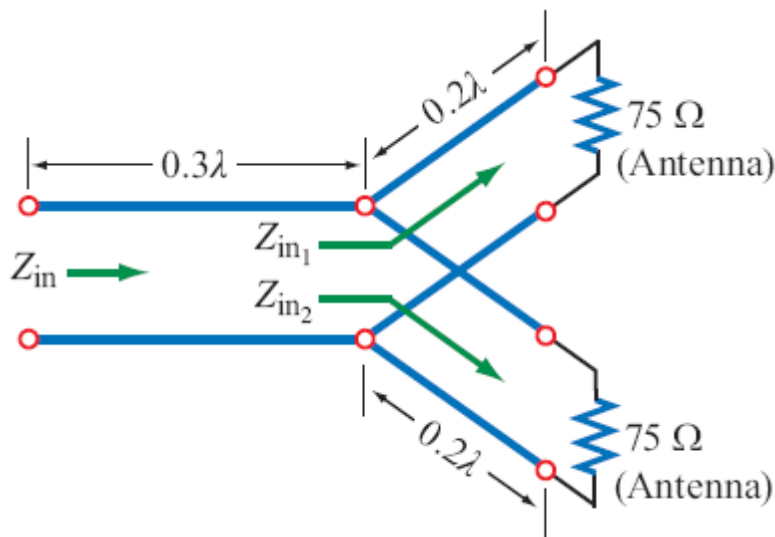
**Fig. P3:** Transmission line model.

- [P4] A lossless transmission line of electrical length  $l = 0.35\lambda$  is terminated in a load impedance as shown in Fig. P4. Find  $\Gamma_L$ , SWR,  $\Gamma_{in}$  and  $Z_{in}$ .



**Fig. P4:** Circuit for Problem P4.

[P5] Two half-wave dipole antennas, each with an impedance of  $75 \Omega$ , are connected in parallel through a pair of transmission lines, and the combination is connected to a feed transmission line, as shown in Fig. P5.

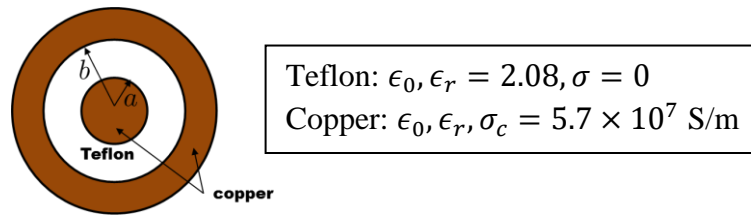


**Fig. P5:** Circuit for Problem P5.

All lines are  $50 \Omega$  and lossless.

- Calculate  $Z_{in1}$ , the input impedance of the antenna-terminated line, at the parallel juncture.
- Combine  $Z_{in1}$  and  $Z_{in2}$  in parallel to obtain  $Z'_L$ , the effective load impedance of the feedline.
- Calculate  $Z_{in}$  of the feedline.

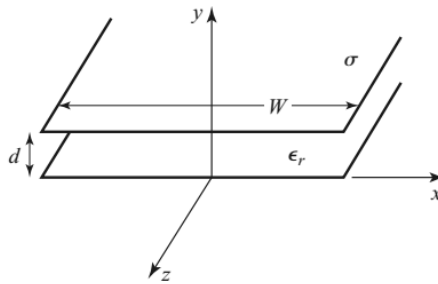
[P6] **2.3** - RG-402U semirigid coaxial cable has an inner conductor diameter of  $0.91 \text{ mm}$  and a dielectric diameter (equal to the inner diameter of the outer conductor) of  $3.02 \text{ mm}$ . Both conductors are copper, and the dielectric material is Teflon.



**Fig. P6:** Coaxial cable T-Line.

- (a) Compute the  $R, L, G$ , and  $C$  parameters of this line at 1 GHz, and use these results to find  $Z_o$  and attenuation of the line at 1 GHz.
- (b) Does it matter how thick the outer conductor is?

[P7] **2.5** - For the parallel plate line shown in Fig. P7, derive the  $R, L, G$ , and  $C$  parameters. Assume  $W \gg d$ .



**Fig. P7:** Parallel plate T-Line.